

# **Beveridge Curve in the Dynamic Model**

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$$\begin{cases} \Theta^* = 1 \\ u^* = \sqrt{uv} \end{cases} \quad \text{requires} \quad \begin{cases} p = 1 & (\text{recruiting cost}) \\ \text{Beveridge curve is hyperbola} \end{cases}$$

Beveridge curve in dynamic model:

$$u(\theta) = \frac{\lambda}{\lambda + f(\theta)}$$

job-separation rate

matching elasticity

$$(=) \quad u = \frac{\lambda}{\lambda + \nu [v/u]^{1-\eta}}$$

$$(=) \quad \lambda u + \nu v^{1-\eta} u^\eta = \lambda$$

$$(=) \quad \nu v^{1-\eta} u^\eta = \lambda(1-u)$$

$$(=) \quad v^{1-\eta} = -\frac{\lambda(1-u)}{\nu u^\eta}$$

$$(=) \quad v(u) = \left[ \frac{\lambda(1-u)}{\nu u^\eta} \right]^{1/(1-\eta)}$$

$$\frac{d \ln v}{d \ln u} = \frac{1}{1-\eta} \left[ -\frac{u}{1-u} - \eta \right] = -\frac{1}{1-\eta} \left[ \eta + \frac{u}{1-u} \right]$$

$$\eta \gg u/1-u$$

so Beveridge curve is  
almost inelastic

$$\begin{cases} u \approx 5\% \\ 1-u \approx 0.95 \\ u/(1-u) \approx 5\% \end{cases}$$

$$\eta \approx 0.5$$

If  $\eta = 0.5$  ( Petrucci & Pissarides 2001)

then  $\frac{d \ln \omega}{d \ln u} = -2 \left( 0.5 + \frac{u}{1-u} \right) = -\left( 1 + \frac{u}{1-u} \right)$

$$\frac{d \ln \omega}{d \ln u}$$

$$\approx -1$$

To have hyperbola at efficiency point.

set  $\gamma$  such that  $\frac{\eta}{1-\eta} + \frac{u^*}{(1-\eta)(1-u^*)} = 1$

$$u^* = u \% \rightarrow \frac{\gamma}{1-\gamma} + \frac{0.04}{(1-\gamma) \times 0.96} = 1$$

$$\rightarrow \boxed{\gamma \approx 0.44}$$